

Staging 15 Years Later

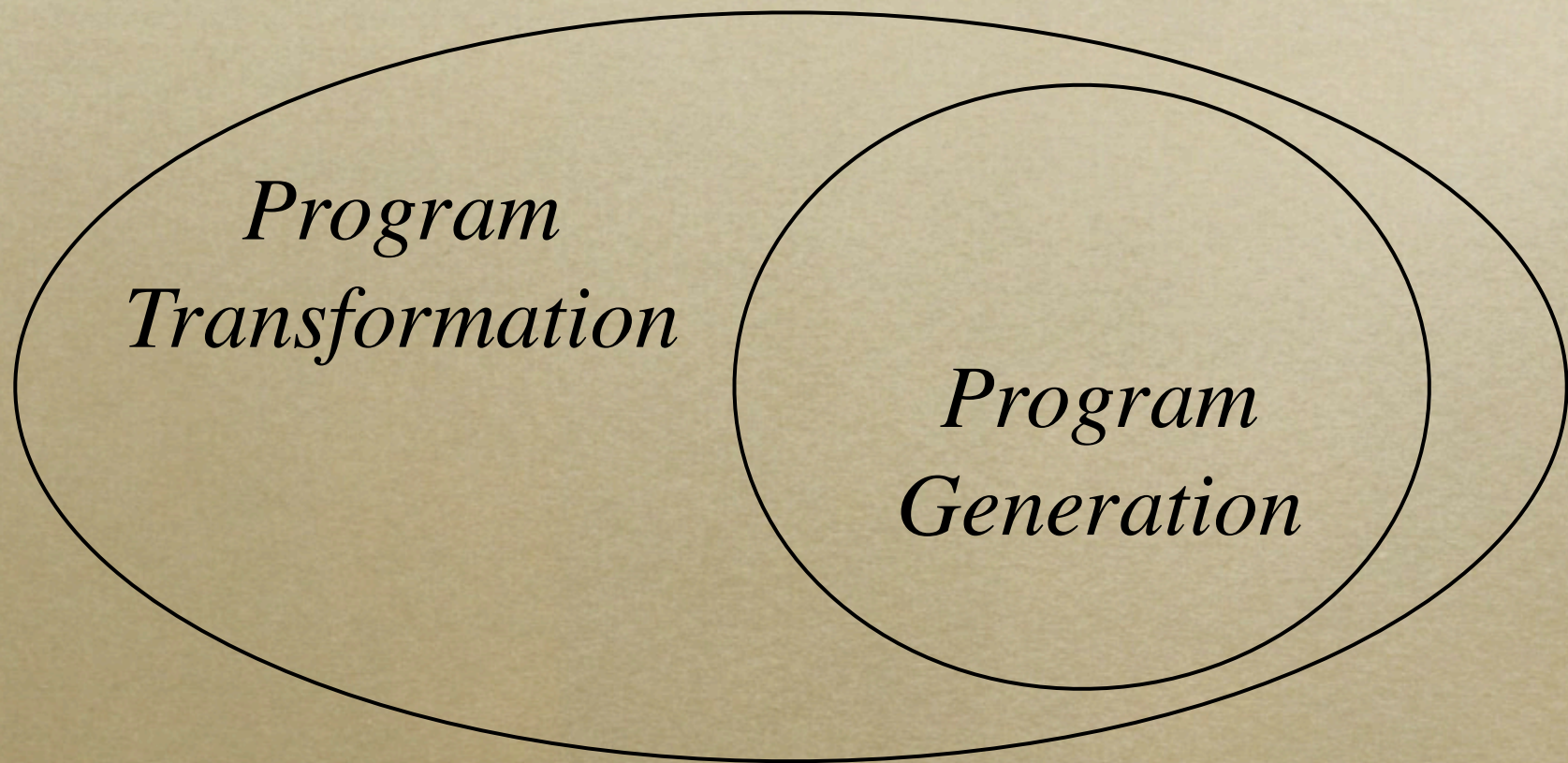
Walid Taha

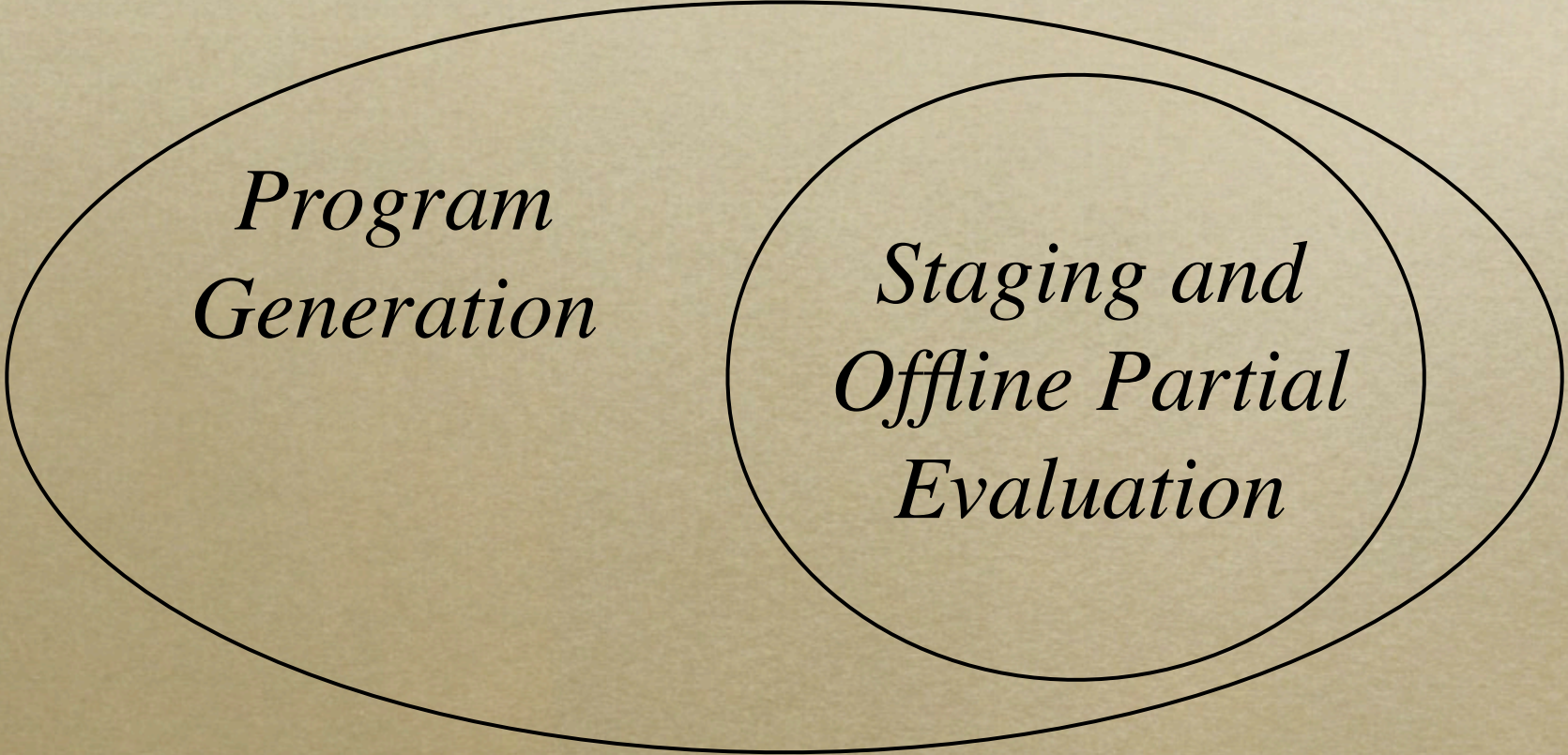
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About “Walid”

- *94-99: PhD at OGI w/ Prof. Sheard*
- *99-00: Post-doc at Chalmers, w/ Prof. Hughes*
- *00-02: Researcher, Yale, w/ Prof. Hudak*
- *02-10: Assistant Professor at Rice*
- *10-: Professor at Halmstad*

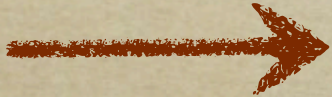




*Program
Generation*

*Staging and
Offline Partial
Evaluation*

Staging *a la* 1997

<i>Program</i> 	<i>Staged or Annotated Program</i>
$a = 1$	$a = 1$
$b = 2$	$b = 2$
$c = 3$	$c = 3$
$d = (x+a)-(b*c)$	$d = \text{run } \textcolor{blue}{“(x+a) - `(lift (b*c))”}$
<i>... at runtime</i>	<i>... at runtime (2nd stage)</i>
$d = (x+a)-(\underline{b*c})$	$d = (x+1)-\underline{6}$

Since then

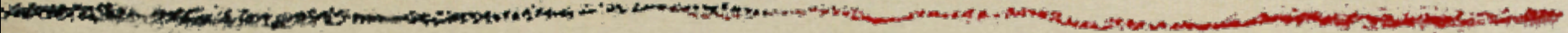
- *Implementations*: *MetaML*, *MetaOCaml*, *Template Haskell*, *Java Mint*, *BER MetaOCaml*, *ConCoqtion*, *lightweight staging libraries*, ...
- *Type systems and semantics*: *Lots!*
- *Programming*: *Tag-less staged interp's*, *monadic staging*, *abstract interpretation*

Today

- Lots *technical results* amassed!
 - Semantics, type systems, formal reasoning principles, implementation techniques, programming case studies
- Stepping back, what's *emerging picture*?


This Talk

- *Staging as an optimization*
- *Staging and partial evaluation*
- *Things that stage well*
- *The perfect language for staging*
- *What staging types actually do*
- *Conclusion and Challenges*



Staging as an Optimization

Partial Evaluation



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Partial evaluation

From Wikipedia, the free encyclopedia

Not to be confused with [partial application](#).

In [computing](#), **partial evaluation** is a technique for several different types of [program optimization](#) by [specialization](#). The most straightforward application is to produce new programs which [run faster](#) than the originals while being guaranteed to behave in the same way.

Traditional view

- *Given the program*
 - `power(x,n) = if n=1 then
x else x*power(x,n-1)`
- *Partial evaluate for n=2*
 - `power2(x) = x*x`
- *Reusability **and** performance!*

What happens in practice

- *Programmer writes*
 - `square(x) = x*x`
 - `cube(x) = x*x*x`
 - `fourthPower(x) = x*x*x*x`
- *Eventually, programmer scratches head*
- *Programmer says “Naaah”. Moves on*

Staging as an optimization

- *Partial evaluation and staging can be great optimizations, but they often work best on programs **that just don't exist yet***
- *Creating **stageable** programs is tricky, and is still, in most cases, **a big investment. Usually, too big...***

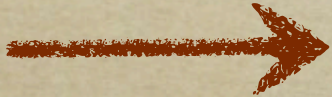
Staging and evaluation order

- *Staging is about very fine control over evaluation order in programs*
- *Traditional strategies*
 - *CBV, CBN only evaluate closed code*
- *What if you want to be MORE strict?*
- *Go under binders. Introduces open code*



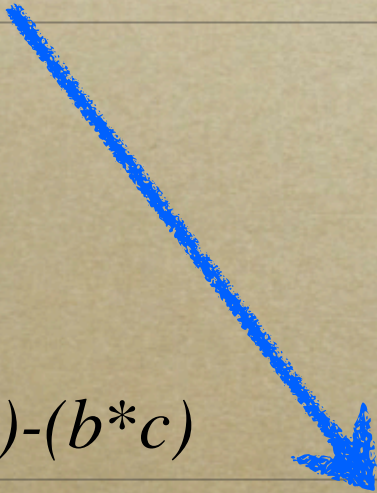
Staging and Partial Evaluation

Staging *a la* 1997

<i>Program</i> 	<i>Staged or Annotated Program</i>
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$d = (x+a)-(\underline{b*c})$	$d = (x+1)-\underline{6}$

Partial Evaluation *a la* 1985

<i>Program</i>	<i>Binding-Time Annotations</i>
$a = 1$	$a = 1$
$b = 2$	$b = 2$
$c = 3$	$c = 3$
$d = (x+a)-(b*c)$	$d = \text{run } \textcolor{violet}{“(x+a) - `(lift (b*c))”}$
<i>... at runtime</i>	<i>Specialized Program</i>
$d = (x+a)-(\underline{b*c})$	$d = (x+1)-\underline{6}$

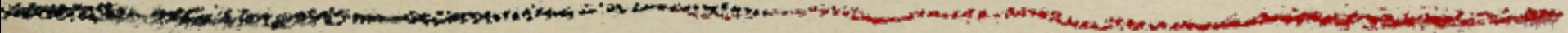


The Paradox

- Staging *cannot do more* than partial evaluation (PE)
- Staging is *less automatic* than offline partial evaluation. It's *manual* binding time analysis

Staging vs. partial evaluation

- *Traditionally, when “a program did not partial evaluate right”, it was hard to figure out why. Manual staging seems to*
 - *help explain to users how partial evaluation works*
 - *help users study the stageability of algorithms*



Things that stage well



Stylized Interpreters

What is an interpreter?

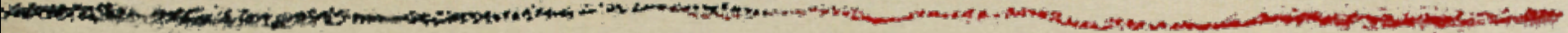
- *It's a pattern!*
 - *Early input (program)*
 - *Late, varying input (the data)*
- *PLs, DSLs, runtime reflection, FFTW*
- *Hygienic macros, HDLs*
- *Software libraries*

Stylized how?

- *We need it to be stageable*
- *Classic: “What not to do when writing an interpreter for staging”, 1996*
- *Denotationally compositional*
- *“Looks like a translation if you squint”*
- *Already in monadic or CPS style*

Hands on tutorial exist

- *“Gentle introduction to multi-stage programming (Parts I and II)”*
- *“DSL implementation in MetaOCaml, Template Haskell, and C++”*



The perfect language for staging



MetaHaskell

Why Haskell?

- *Purely functional, no side effects*
 - *A safe, fully static type system exists*
- *Lazy*
 - *Simplifies reasoning about staging*
- *Monads*
- *Very rich type system*

What needs to be done?

- *Convince Simon Peyton Jones :-)*
- *Need to identify research challenges*
 - *Gradual-typing based approach*
 - *Combine Template Haskell & MSP*
 - *Checking soundness w/ full typ. sys.*
 - *Runtime code generation*



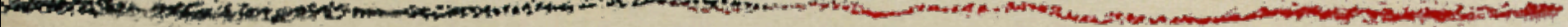
What staging types actually do

How staging types work

- *Types:* $s, t ::= \mathbf{int} \mid t * t \mid t + t \mid t^{\wedge} t \mid \langle t \rangle$
- *The curious facts*
 - $\mathbf{int} \sim/\sim \langle \mathbf{int} \rangle$, but we have $\langle \mathbf{int} \rangle^{\wedge} \mathbf{int}$
 - $\langle s * t \rangle \sim\sim \langle s \rangle * \langle t \rangle$
 - $\langle s^{\wedge} t \rangle \sim\sim \langle s \rangle^{\wedge} \langle t \rangle$
 - *and sometimes:* $\langle s + t \rangle \sim\sim \langle s \rangle + \langle t \rangle$

What staging types really do

- *The code type flows to the leaves*
 - *This provides a normal form*
- *A lot like basic unit checking in physics*
- *Provide a great basis for programming with abstract interpretation*



Conclusion

Summary

- *Staging is useful because it helps us analyze the **stageability** of algorithms*
- ***Interpreters** are the “killer app”*
- ***Haskell** is the ideal staging language*
- *Staged types flow to **leaves of types***
- ***Stageability** is like **basic unit checking***

Challenges

- *Existential questions (re indexed types)*
 - *Is staging (MSP) really necessary*
 - *Is it enough?*
- *SML: Standard Macro Language*
 - *Extensible grammar, type system*
 - *Language independent*

Challenges

- *Type safe staging w/shared mutable state*
 - *SOA: Separability-based type system*
 - *Question: Do we REALLY need it?*
- *Type safe runtime code generation*
- *Computer-aided stageability analysis*
- *Compiler/architecture code-design*

Challenges

- *Mathematical equations, esp. hybrid differential equations. Example:*

$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{x}_i} \right) = \frac{\partial L}{\partial x_i} \quad (1 \leq i \leq N).$$

- *Preliminary results quite promising*

Concrete milestone challenges

- *MSP-based FFT that beats FFT(E/W)*
- *Matrix operations that beats BLAS*
- *MSP-based BED formal tools*
- *MSP-based NAS-parallel benchmarks*
- *MSP-based TCE-engine benchmarks*